# CoCoA-5 - Feature #7

# Automatic mapping between (some) rings

20 Oct 2011 11:48 - Anna Maria Bigatti

Status:ResolvedStart date:20 Oct 2011Priority:HighDue date:

Assignee: Anna Maria Bigatti % Done: 80%

Category: Parser/Interpreter Estimated time: 0.00 hour

Target version: CoCoA-5.4.2 Spent time: 7.00 hours

# **Description**

There are a few obvious cases, i.e. those for which there is a "single step" homomorphism, for example:

RingZ --> R RingQ --> R R --> R/I

 $R \rightarrow R[x,y,z]$ 

AMB 2012 added matrix(R, M) to CoCoA-5 for automatic mapping AMB 2013 added RingElem(R, a) to CoCoA-5 for automatic mapping

AMB 2014 added ReadExpr(R, "...") to CoCoA-5 for reading an explicit expression

## Related issues:

Related to CoCoALib - Feature #223: Automatic mapping of RingElems	Closed	08 Aug 2012
Related to CoCoALib - Feature #151: Iterated CanonicalHom	New	03 May 2012
Related to CoCoA-5 - Bug #100: BringIn should map only the indets in its arg	New	07 Mar 2012
Related to CoCoA-5 - Bug #132: BringIn should allow reduction modulo p	Closed	17 Apr 2012
Related to CoCoA-5 - Feature #309: (Multi)BlockMatrix	Closed	13 Feb 2013
Related to CoCoA-5 - Design #483: Unique copies of rings in CoCoA-5	New	19 Mar 2014
Related to CoCoALib - Feature #209: ReadExpr: input polynomials in CoCoALib	Closed	24 Jul 2012
Related to CoCoA-5 - Design #634: Symbol in the coeff ring	Rejected	22 Oct 2014
Related to CoCoA-5 - Design #635: Automatic mapping of RingElem (in operation	Closed	22 Oct 2014
Related to CoCoA-5 - Design #636: Distinguish indets from symbols in coeffrin	Rejected	23 Oct 2014
Related to CoCoA-5 - Design #637: Undesirable consequence of automatic mappin	Closed	23 Oct 2014
Related to CoCoALib - Feature #645: Automatic mapping of RingElem: user selec	Rejected	04 Nov 2014
Related to CoCoALib - Feature #1132: Canonical homomorphism for (some) polyno	New	30 Nov 2017
Related to CoCoALib - Feature #738: Extend homomorphism to polynomial ring	In Progress	25 Jun 2015
Related to CoCoALib - Design #1085: Fns with "OUT" args: should they give ERR	Closed	30 Jun 2017
Related to CoCoA-5 - Feature #1461: Automatic mapping for multiplication?	Closed	10 Jun 2020
Related to CoCoALib - Design #1414: Make class RingElemVector?	In Progress	12 Feb 2020
Related to CoCoA-5 - Design #1493: Automatic ring mapping in assignment?	Closed	28 Sep 2020
Related to CoCoALib - Design #1515: Indets in coeffring are ringelems in coef	Rejected	22 Oct 2020

## History

## #1 - 08 Nov 2011 16:41 - John Abbott

JAA thinks that a good design approach would be to produce a function which takes as args two rings, and returns a **RingHom** (and not a partial ring hom) which must be applied to map elements of the "simpler" ring into the other ring. The domain and codomain of the ringhom will indicate which value(s) is/are to be mapped.

JAA is not sure what the function should do if no automatic mapping is supported between the two rings. There are two obvious alternatives: throw an exception, or return a boolean (in addition to the RingHom).

JAA is not sure what the function should do if the two rings supplied are equal -- it could return the identity RingHom or it could give an error. At the moment giving an error seems the better option.

23 Apr 2024 1/5

### #2 - 15 Nov 2011 14:00 - Anna Maria Bigatti

- Category set to Parser/Interpreter

### #3 - 23 Mar 2012 14:41 - John Abbott

Probably the simplest definition is simply that R1 is "simpler" than R2 if the construction of R2 passed explicitly via that of R1.

For instance this means that R is always regarded as being simpler than the quotient R/I.

## #4 - 30 May 2012 13:09 - Anna Maria Bigatti

Proposal for new "constructors": R ring, A matrix, x ringelem (or powerproduct or ...), ... and what else?

# Mat(R, A), RingElem(R, x)

checks if object is mappable into R and returns its image in R: equivalent to

```
phi := CanonicalHom(RingOf(object), R);
apply(phi, object)
```

Automatic ring in operations is in general very difficult to detect.

Making these new constructors available might be a good and clean intermediate solution.

These "constructors" may be made available in CoCoALib too, but that implies including CanonicalHom.H in all .C files offering them.

# #5 - 30 May 2012 16:08 - John Abbott

It would be handy to have a similar shortcut for homogeneous lists.

Also for ideals, but that raises the same question that came up for **BringIn**.

The doc for BringIn says that it works for ringelems and matrices, lists and vectors but **not** ideals.

The CoCoALib fn apply does not appear to be documented!

# #6 - 25 Sep 2012 16:14 - John Abbott

- Status changed from New to In Progress
- Assignee set to Anna Maria Bigatti
- % Done changed from 0 to 10

### #7 - 04 Oct 2012 12:12 - John Abbott

Assignment of an integer (or rational) to a RingElem will automatically map into the ring.

However, we want to be cautious about extending this automatic mapping to other types of assignment, especially since assignment from a RingElem belonging to another ring does not perform automatic mapping.

23 Apr 2024 2/5

### #8 - 15 Feb 2013 11:46 - Anna Maria Bigatti

- Target version set to CoCoA-5.0.9

### #9 - 05 Dec 2013 11:47 - John Abbott

Renzo reminds us that this task is important!

## #10 - 21 Mar 2014 11:48 - Anna Maria Bigatti

- Target version changed from CoCoA-5.0.9 to CoCoA-5.1.0 Easter14

## #11 - 09 Apr 2014 17:38 - John Abbott

- Target version changed from CoCoA-5.1.0 Easter14 to CoCoA-5.1.1 Seoul14

## #12 - 27 Aug 2014 18:36 - Anna Maria Bigatti

- Target version changed from CoCoA-5.1.1 Seoul14 to CoCoA-5.1.2 summer 2015
- % Done changed from 10 to 30

# #13 - 11 May 2015 14:53 - John Abbott

- Target version changed from CoCoA-5.1.2 summer 2015 to CoCoA-5.1.3/4 Jan 2016

### #14 - 17 Feb 2016 11:35 - John Abbott

- Target version changed from CoCoA-5.1.3/4 Jan 2016 to CoCoA-5.2.0 spring 2017

I am "bumping" this issue by 1 version of CoCoA-5. It is marked as "high" priority, but has not been worked on for 3-4 years (no doubt because it is tricky).

Whether we'll really be able to deal with it for the next version remains to be seen.

## #15 - 13 Oct 2016 17:25 - John Abbott

No chance of finishing this is in the near future; postponing by 1 version.

# #16 - 13 Oct 2016 17:25 - John Abbott

- Target version changed from CoCoA-5.2.0 spring 2017 to CoCoA-5.2.2

# #17 - 15 Nov 2017 17:41 - John Abbott

- Target version changed from CoCoA-5.2.2 to CoCoA-5.2.4

# #18 - 30 Nov 2017 10:00 - John Abbott

- Related to Feature #1132: Canonical homomorphism for (some) polynomial rings? added

### #19 - 30 Nov 2017 10:02 - John Abbott

- Related to Feature #738: Extend homomorphism to polynomial ring added

## #20 - 25 Jul 2018 17:15 - John Abbott

- Target version changed from CoCoA-5.2.4 to CoCoA-5.3.0

### #21 - 01 Oct 2019 14:54 - John Abbott

- Target version changed from CoCoA-5.3.0 to CoCoA-5.4.0

23 Apr 2024 3/5

#### #22 - 20 Jun 2020 21:25 - John Abbott

- Related to Design #1085: Fns with "OUT" args: should they give ERR::MixedRings? added

### #23 - 20 Jun 2020 21:33 - John Abbott

- % Done changed from 30 to 50

I have partly implemented this (in CoCoALib) after discussions wirh Anna (who is uncertain about some aspects).

### #24 - 20 Jun 2020 21:34 - John Abbott

- Related to Feature #1461: Automatic mapping for multiplication? added

### #25 - 22 Jun 2020 18:00 - John Abbott

- Related to Design #1414: Make class RingElemVector? added

### #26 - 28 Sep 2020 16:40 - John Abbott

- Related to Design #1493: Automatic ring mapping in assignment? added

### #27 - 22 Oct 2020 17:23 - John Abbott

- Related to Design #1515: Indets in coeffring are ringelems in coeffring? added

### #28 - 27 Oct 2020 18:43 - John Abbott

- % Done changed from 50 to 60

I have decided to make this the "master issue" for questions related to automatic ring conversion (mainly because it is the oldest).

Here is a summary of the main points:

- after use P all symbols in P are made available as ringelems in P (even if the symbol lies in a subring) -- see #1515 (and #636)
- no automatic mapping of RingElems for equality tests (throws MixedRings exception instead) -- see #637
- fns with OUT params (of ringelem type) do not require that the ring of the OUT param be "correct": the right ring will be set by the call (the same way that assignment sets the right ring) -- see #1085 (and #1500 comment 10)

## Automatic mapping applies only to single values

- not to matrices (even if 1x1)
- see issue #635
- issue #1493 lets a single value be "promoted" when being assigned to matrix element; but the assignment cannot "promote" the matrix.

# #29 - 27 Oct 2020 19:05 - John Abbott

Here are done list and todo list copied from issue #1461 comments 7 & 8. Moving them here.

### **DONE LIST**

- MatrixOps.C
- MatrixOps-KroneckerProd.C
- module.C (mostly)

# **TODO LIST**

23 Apr 2024 4/5

- DenseMat: myRowMul, myColMul, myAddRowMul, myAddColMul
- FieldIdeal -- needs vector of RingElem in same ring
- ideal.C many, some need vector of RingElem in same ring
- Matrix.C for SetEntry, also lamEqual
- MatrixSpecial.C for JacobianMat which needs vector of RingElem in same ring
- MatrixView many cases, some need vector of RingElem in same ring
- PolyFamilies for DicksonPoly
- ring.C for operator+= and so on
- RingElemOps-CoprimeFactorBasis needs vector RingElem from same ring.
- SparsePolyOps-XXX many

## #30 - 03 Feb 2022 19:32 - John Abbott

- Target version changed from CoCoA-5.4.0 to CoCoA-5.4.2

### #31 - 10 Mar 2023 17:08 - John Abbott

- Status changed from In Progress to Resolved
- % Done changed from 60 to 80

What is the status of this issue? I thought it was almost finished.

23 Apr 2024 5/5