CoCoA-5 - Feature \#7
Automatic mapping between (some) rings
20 Oct 2011 11:48 - Anna Maria Bigatti

| Status: | Resolved | Start date: | 20 Oct 2011 |
| :--- | :--- | :--- | :--- |
| Priority: | High | Due date: |  |
| Assignee: | Anna Maria Bigatti | \% Done: | $80 \%$ |
| Category: | Parser/Interpreter | Estimated time: | 0.00 hour |
| Target version: | CoCoA-5.4.2 | Spent time: | 7.00 hours |

## Description

There are a few obvious cases, i.e. those for which there is a "single step" homomorphism, for example:
RingZ --> R
RingQ --> R
R --> R/l
$R$--> $R[x, y, z]$
AMB 2012 added matrix(R, M) to CoCoA-5 for automatic mapping
AMB 2013 added RingElem(R, a) to CoCoA-5 for automatic mapping
AMB 2014 added ReadExpr(R, "...") to CoCoA-5 for reading an explicit expression

## Related issues:

Related to CoCoALib - Feature \#223: Automatic mapping of RingElems
Related to CoCoALib - Feature \#151: Iterated CanonicalHom
Related to CoCoA-5 - Bug \#100: Bringln should map only the indets in its arg
Related to CoCoA-5 - Bug \#132: BringIn should allow reduction modulo p
Related to CoCoA-5 - Feature \#309: (Multi)BlockMatrix
Related to CoCoA-5 - Design \#483: Unique copies of rings in CoCoA-5
Related to CoCoALib - Feature \#209: ReadExpr: input polynomials in CoCoALib
Related to CoCoA-5 - Design \#634: Symbol in the coeff ring
Related to CoCoA-5 - Design \#635: Automatic mapping of RingElem (in operation...
Related to CoCoA-5 - Design \#636: Distinguish indets from symbols in coeffrin...
Related to CoCoA-5 - Design \#637: Undesirable consequence of automatic mappin...
Related to CoCoALib - Feature \#645: Automatic mapping of RingElem: user selec...
Related to CoCoALib - Feature \#1132: Canonical homomorphism for (some) polyno...
Related to CoCoALib - Feature \#738: Extend homomorphism to polynomial ring
Related to CoCoALib - Design \#1085: Fns with "OUT" args: should they give ERR...
Related to CoCoA-5 - Feature \#1461: Automatic mapping for multiplication?
Related to CoCoALib - Design \#1414: Make class RingElemVector?
Related to CoCoA-5 - Design \#1493: Automatic ring mapping in assignment?
Related to CoCoALib - Design \#1515: Indets in coeffring are ringelems in coef...

| Closed | 08 Aug 2012 |
| :--- | :--- |
| New | 03 May 2012 |
| New | 07 Mar 2012 |
| Closed | 17 Apr 2012 |
| Closed | 13 Feb 2013 |
| New | 19 Mar 2014 |
| Closed | 24 Jul 2012 |
| Rejected | 22 Oct 2014 |
| Closed | 22 Oct 2014 |
| Rejected | 23 Oct 2014 |
| Closed | 23 Oct 2014 |
| Rejected | 04 Nov 2014 |
| New | 30 Nov 2017 |
| In Progress | 25 Jun 2015 |
| Closed | 30 Jun 2017 |
| Closed | 10 Jun 2020 |
| In Progress | 12 Feb 2020 |
| Closed | 28 Sep 2020 |
| Rejected | 22 Oct 2020 |

## History

\#1-08 Nov 2011 16:41 - John Abbott
JAA thinks that a good design approach would be to produce a function which takes as args two rings, and returns a RingHom (and not a partial ring hom) which must be applied to map elements of the "simpler" ring into the other ring. The domain and codomain of the ringhom will indicate which value(s) is/are to be mapped.

JAA is not sure what the function should do if no automatic mapping is supported between the two rings. There are two obvious alternatives: throw an exception, or return a boolean (in addition to the RingHom).

JAA is not sure what the function should do if the two rings supplied are equal -- it could return the identity RingHom or it could give an error. At the moment giving an error seems the better option.

## \#2-15 Nov 2011 14:00-Anna Maria Bigatti

- Category set to Parser/Interpreter


## \#3-23 Mar 2012 14:41 - John Abbott

Probably the simplest definition is simply that R1 is "simpler" than R2 if the construction of R2 passed explicitly via that of R1.

For instance this means that $R$ is always regarded as being simpler than the quotient $R / I$.

## \#4-30 May 2012 13:09-Anna Maria Bigatti

Proposal for new "constructors": R ring, A matrix, x ringelem (or powerproduct or ...), ... and what else?
$\operatorname{Mat}(\mathrm{R}, \mathrm{A})$, RingElem(R, $\mathbf{x})$
checks if object is mappable into $\mathbf{R}$ and returns its image in $\mathbf{R}$ : equivalent to
phi := CanonicalHom(RingOf(object), R);
apply(phi, object)

Automatic ring in operations is in general very difficult to detect.
Making these new constructors available might be a good and clean intermediate solution.

These "constructors" may be made available in CoCoALib too, but that implies including CanonicalHom.H in all .C files offering them.

## \#5 - 30 May 2012 16:08 - John Abbott

It would be handy to have a similar shortcut for homogeneous lists.
Also for ideals, but that raises the same question that came up for Bringln.

The doc for Bringln says that it works for ringelems and matrices, lists and vectors but not ideals.
The CoCoALib fn apply does not appear to be documented!

## \#6-25 Sep 2012 16:14 - John Abbott

- Status changed from New to In Progress
- Assignee set to Anna Maria Bigatti
- \% Done changed from 0 to 10


## \#7-04 Oct 2012 12:12- John Abbott

Assignment of an integer (or rational) to a RingElem will automatically map into the ring.
However, we want to be cautious about extending this automatic mapping to other types of assignment, especially since assignment from a RingElem belonging to another ring does not perform automatic mapping.

## \#8-15 Feb 2013 11:46 - Anna Maria Bigatti

- Target version set to CoCoA-5.0.9


## \#9-05 Dec 2013 11:47- John Abbott

Renzo reminds us that this task is important!

## \#10-21 Mar 2014 11:48-Anna Maria Bigatti

- Target version changed from CoCoA-5.0.9 to CoCoA-5.1.0 Easter14


## \#11-09 Apr 2014 17:38- John Abbott

- Target version changed from CoCoA-5.1.0 Easter14 to CoCoA-5.1.1 Seoul14


## \#12-27 Aug 2014 18:36-Anna Maria Bigatti

- Target version changed from CoCoA-5.1.1 Seoul14 to CoCoA-5.1.2 summer 2015
- \% Done changed from 10 to 30
\#13-11 May 2015 14:53-John Abbott
- Target version changed from CoCoA-5.1.2 summer 2015 to CoCoA-5.1.3/4 Jan 2016


## \#14-17 Feb 2016 11:35-John Abbott

- Target version changed from CoCoA-5.1.3/4 Jan 2016 to CoCoA-5.2.0 spring 2017

I am "bumping" this issue by 1 version of CoCoA-5. It is marked as "high" priority, but has not been worked on for 3-4 years (no doubt because it is tricky).

Whether we'll really be able to deal with it for the next version remains to be seen.

## \#15-13 Oct 2016 17:25-John Abbott

No chance of finishing this is in the near future; postponing by 1 version.

## \#16-13 Oct 2016 17:25-John Abbott

- Target version changed from CoCoA-5.2.0 spring 2017 to CoCoA-5.2.2


## \#17-15 Nov 2017 17:41 - John Abbott

- Target version changed from CoCoA-5.2.2 to CoCoA-5.2.4


## \#18-30 Nov 2017 10:00-John Abbott

- Related to Feature \#1132: Canonical homomorphism for (some) polynomial rings? added


## \#19-30 Nov 2017 10:02-John Abbott

- Related to Feature \#738: Extend homomorphism to polynomial ring added


## \#20-25 Jul 2018 17:15 - John Abbott

- Target version changed from CoCoA-5.2.4 to CoCoA-5.3.0


## \#21-01 Oct 2019 14:54-John Abbott

- Target version changed from CoCoA-5.3.0 to CoCoA-5.4.0
- Related to Design \#1085: Fns with "OUT" args: should they give ERR::MixedRings? added


## \#23-20 Jun 2020 21:33-John Abbott

- \% Done changed from 30 to 50

I have partly implemented this (in CoCoALib) after discussions wirh Anna (who is uncertain about some aspects).

## \#24-20 Jun 2020 21:34-John Abbott

- Related to Feature \#1461: Automatic mapping for multiplication? added


## \#25-22 Jun 2020 18:00-John Abbott

- Related to Design \#1414: Make class RingElemVector? added


## \#26-28 Sep 2020 16:40-John Abbott

- Related to Design \#1493: Automatic ring mapping in assignment? added


## \#27-22 Oct 2020 17:23 - John Abbott

- Related to Design \#1515: Indets in coeffring are ringelems in coeffring? added


## \#28-27 Oct 2020 18:43-John Abbott

- \% Done changed from 50 to 60

I have decided to make this the "master issue" for questions related to automatic ring conversion (mainly because it is the oldest).
Here is a summary of the main points:

- after use $\mathbf{P}$ all symbols in $P$ are made available as ringelems in $P$ (even if the symbol lies in a subring) -- see \#1515 (and \#636)
- no automatic mapping of RingElems for equality tests (throws MixedRings exception instead) -- see \#637
- fns with OUT params (of ringelem type) do not require that the ring of the OUT param be "correct": the right ring will be set by the call (the same way that assignment sets the right ring) -- see \#1085 (and \#1500 comment 10)


## Automatic mapping applies only to single values

- not to matrices (even if $1 \times 1$ )
- see issue \#635
- issue \#1493 lets a single value be "promoted" when being assigned to matrix element; but the assignment cannot "promote" the matrix.


## \#29-27 Oct 2020 19:05-John Abbott

Here are done list and todo list copied from issue \#1461 comments $7 \& 8$. Moving them here.

## DONE LIST

- MatrixOps.C
- MatrixOps-KroneckerProd.C
- module.C (mostly)

TODO LIST

- DenseMat: myRowMul, myCoIMul, myAddRowMul, myAddCoIMul
- Fieldldeal -- needs vector of RingElem in same ring
- ideal.C many, some need vector of RingElem in same ring
- Matrix.C for SetEntry, also lamEqual
- MatrixSpecial.C for JacobianMat which needs vector of RingElem in same ring
- MatrixView many cases, some need vector of RingElem in same ring
- PolyFamilies for DicksonPoly
- ring.C for operator+= and so on
- RingElemOps-CoprimeFactorBasis needs vector RingElem from same ring.
- SparsePolyOps-XXX many
\#30-03 Feb 2022 19:32-John Abbott
- Target version changed from CoCoA-5.4.0 to CoCoA-5.4.2
\#31-10 Mar 2023 17:08-John Abbott
- Status changed from In Progress to Resolved
- \% Done changed from 60 to 80

What is the status of this issue?
I thought it was almost finished.

