CoCoALib - Design \#1232

## IsPrime(0)

29 Oct 2018 10:44 - John Abbott

| Status: | Closed | Start date: | 29 Oct 2018 |
| :--- | :--- | :--- | :--- |
| Priority: | Normal | Due date: |  |
| Assignee: | John Abbott | \% Done: | $100 \%$ |
| Category: | Various | Estimated time: | 0.66 hour |
| Target version: | CoCoALib-0.99650 November 2019 | Spent time: | 0.70 hour |

## Description

What should IsPrime(0) do?
Currently it gives error (because arg must be strictly positive).
I ask because I wanted to write a short demo for the students, and wanted to check whether the coeffring of a polyring is a (prime) finite field. I first wrote this:

```
k := CoeffRing(P);
if not(IsField(k)) or not(IsPrime(characteristic(k))) then error(...); endif;
```

These lines will not handle gracefully the case that the coeffring is QQ (or any other field of char 0 ). Instead I would have to write
$\mathrm{k}:=$ CoeffRing ( P );
if not(IsField(k)) or characteristic(k) = 0 or not(IsPrime(characteristic(k))) then error(...); endif;

In fact, CoCoA offers the functions IsFiniteField and LogCardinality, so maybe this issue is pointless?
Anyway, I'd like a brief discussion.
Related issues:
Related to CoCoALib - Feature \#898: New function: cardinality of finite field? $\quad$ In Progress 27 Jun 2016

## History

\#1-29 Oct 2018 15:51 - Anna Maria Bigatti

- \% Done changed from 0 to 10

I'd rather keep the error, as in this case you already have IsFiniteField.
I'm not sure whether one would expect it to be true in all possible situations.

## \#2-29 Oct 2018 17:52-John Abbott

- Status changed from New to Closed
- Assignee set to John Abbott
- \% Done changed from 10 to 100
- Estimated time set to 0.66 h

Indeed, I probably created IsFiniteField exactly for this reason. Also the correct code is clearer to read:

```
    if not(IsFiniteField(k)) or LogCardinality(k) > 1 then error(...)
```

Though I admit that LogCardinality is not the most obvious name; maybe FiniteFieldExtnDeg would be clearer? (FFED is a bit long though)

I confirm that the manual page for IsField refers also to IsFiniteField, so the fn is visible.
So, as Anna says, let's leave it as it is currently. Closing.

## \#3-29 Oct 2018 18:00-Anna Maria Bigatti

John Abbott wrote:
Though I admit that LogCardinality is not the most obvious name; maybe FiniteFieldExtnDeg would be clearer?
yes, it would.
Maybe AlgExtDeg? in principle one could also ask it for $\mathrm{QQ}[\mathrm{x}] /(\mathrm{f})$.

## \#4-29 Oct 2018 18:10-John Abbott

- Related to Feature \#898: New function: cardinality of finite field? added

